



How to Improve Model Robustness? A Distributional-Discrepancy Perspective

Jiacheng Zhang

School of Computing and Information Systems

The University of Melbourne

21 November 2025



- ❑ Background
- ❑ **ICML 2025:** Sample-specific Noise Injection for Diffusion-based Adversarial Purification
- ❑ **ICML 2025:** One Stone, Two Birds: Enhancing Adversarial Defense Through the Lens of Distributional Discrepancy

What is an adversarial example (attack)?

88% Tabby Cat



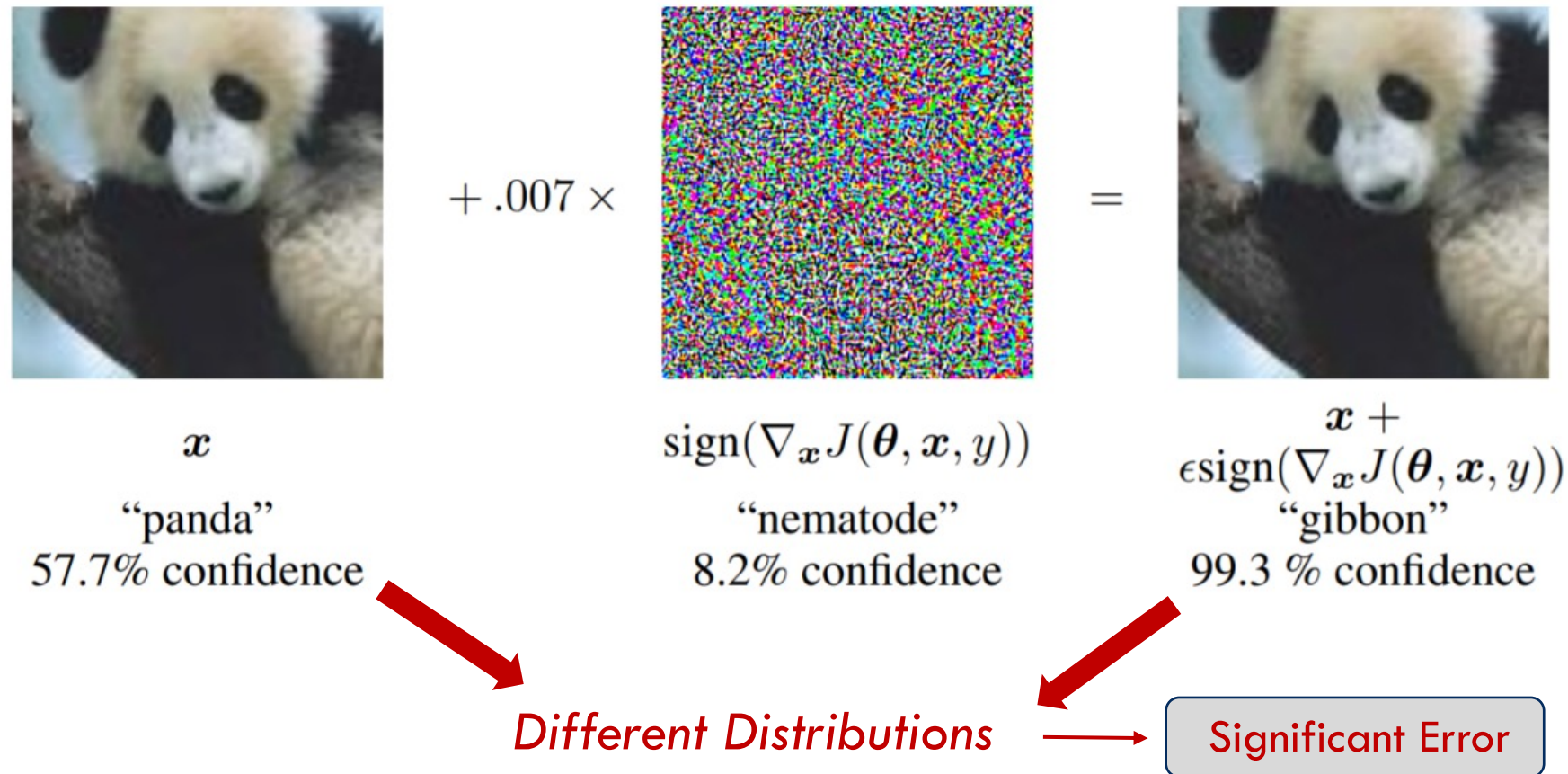
Adversarial
Perturbations →

99% Guacamole

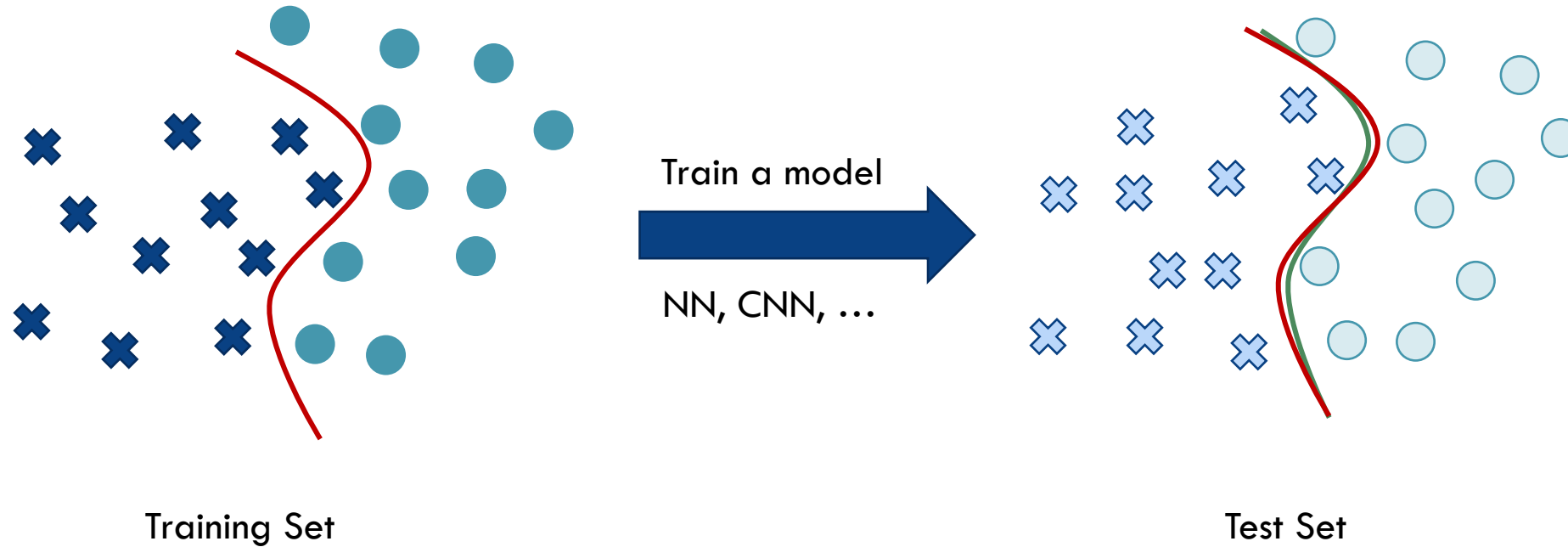


Why it works?

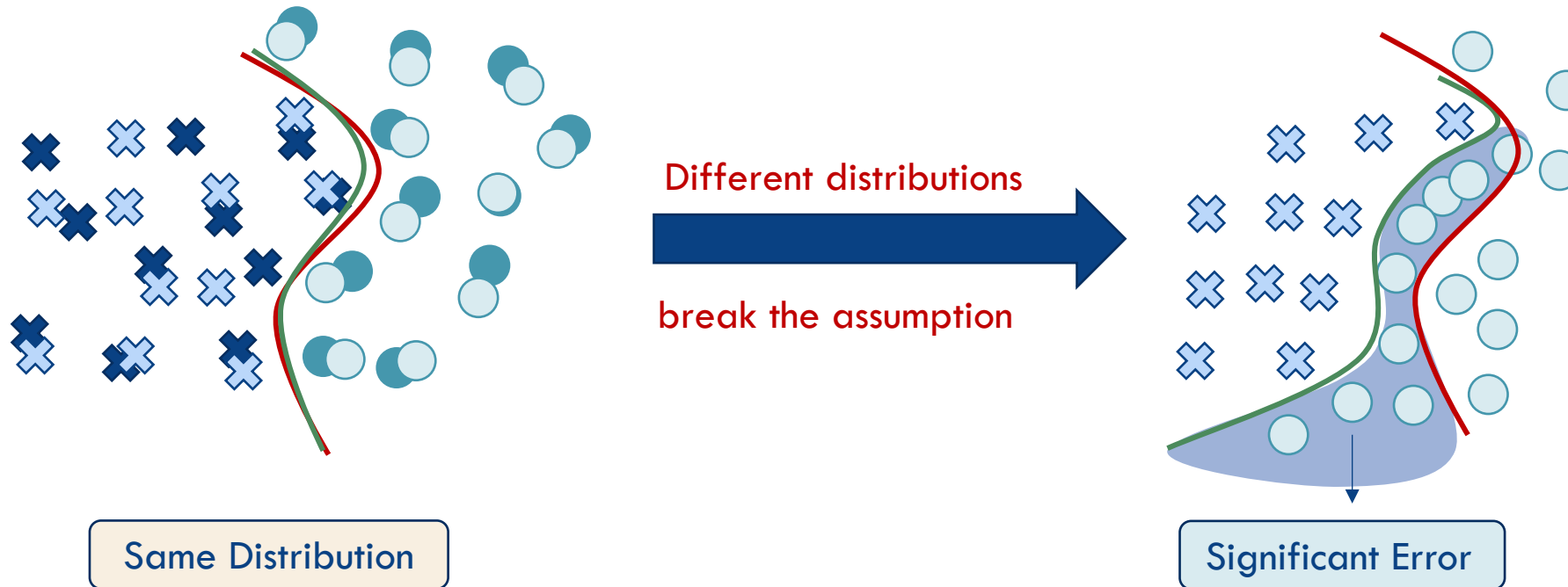
Why adversarial attack can be successful?



Basic assumption in machine learning



Basic assumption in machine learning

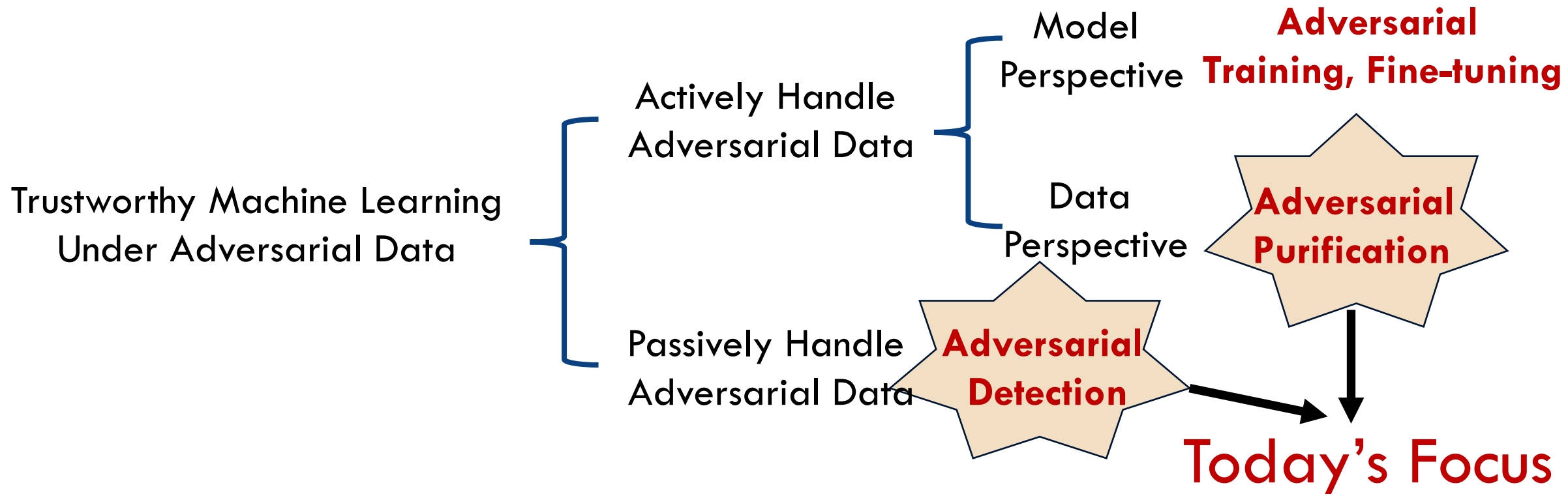


Basic assumption in machine learning

Break the assumption!!!

How to defend against it?

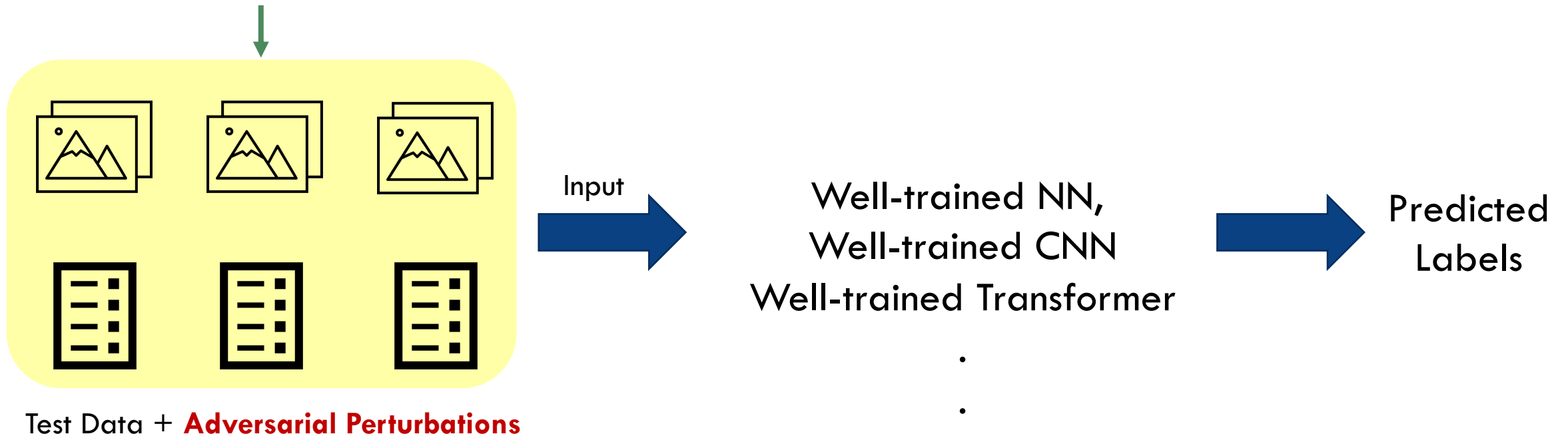
Defend against adversarial attacks



Adversarial detection

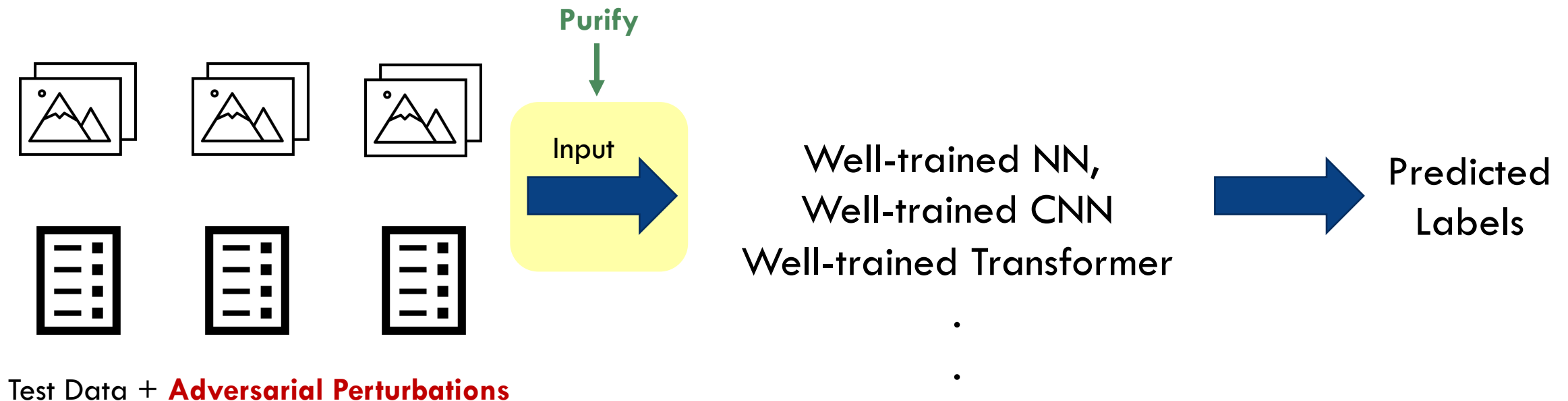
❑ *Adversarial Detection (AD)*: aims to detect and discard AEs.

Discard the adversarial data



Adversarial purification

□ *Adversarial Purification (AP)*: aims to shift AEs back towards their natural counterparts.



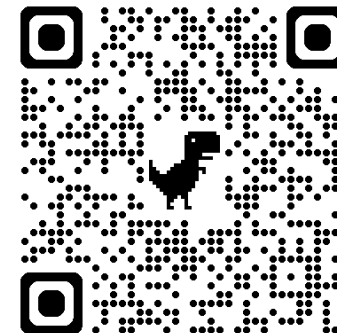
Sample-specific Noise Injection for Diffusion-based Adversarial Purification

Yuhao Sun[^], Jiacheng Zhang[^], Zesheng Ye[^], Chaowei Xiao, Feng Liu^{*}

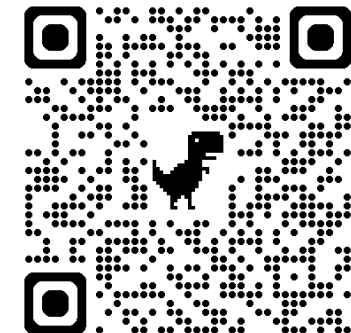
([^] Co-first authors, ^{*} Corresponding authors)

In *ICML*, 2025.

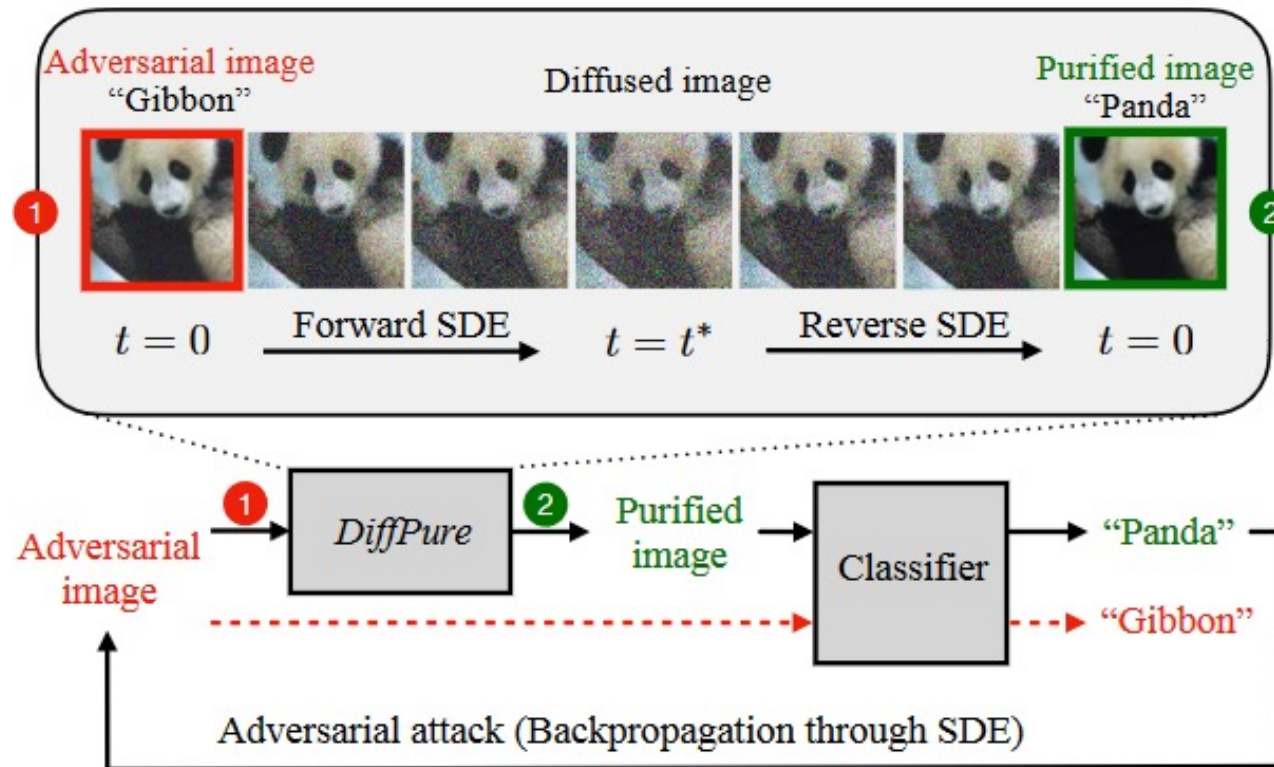
Paper



Code

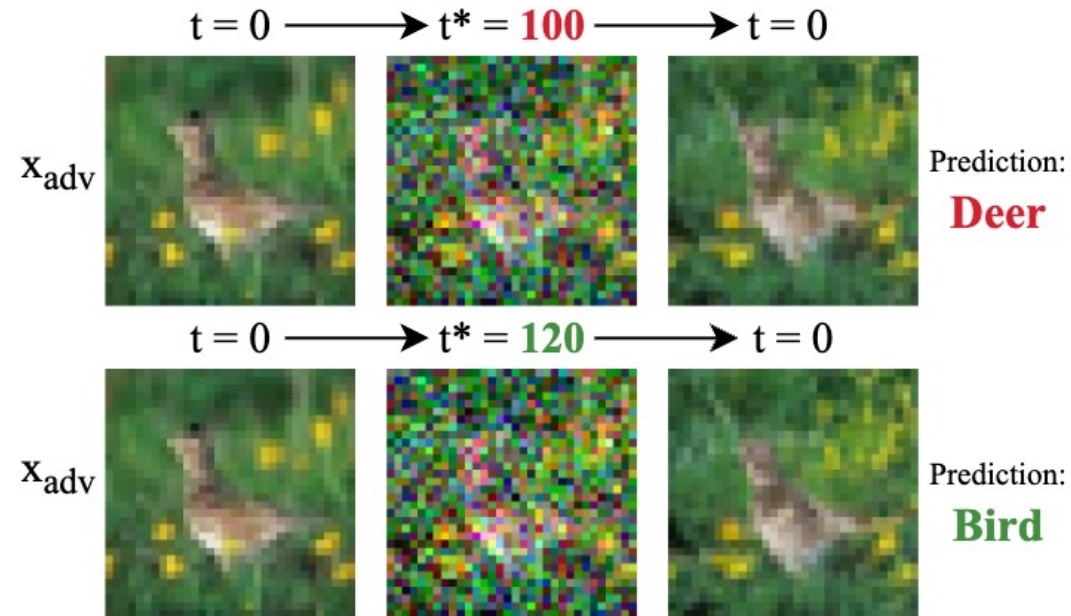


Preliminary: diffusion-based adversarial purification



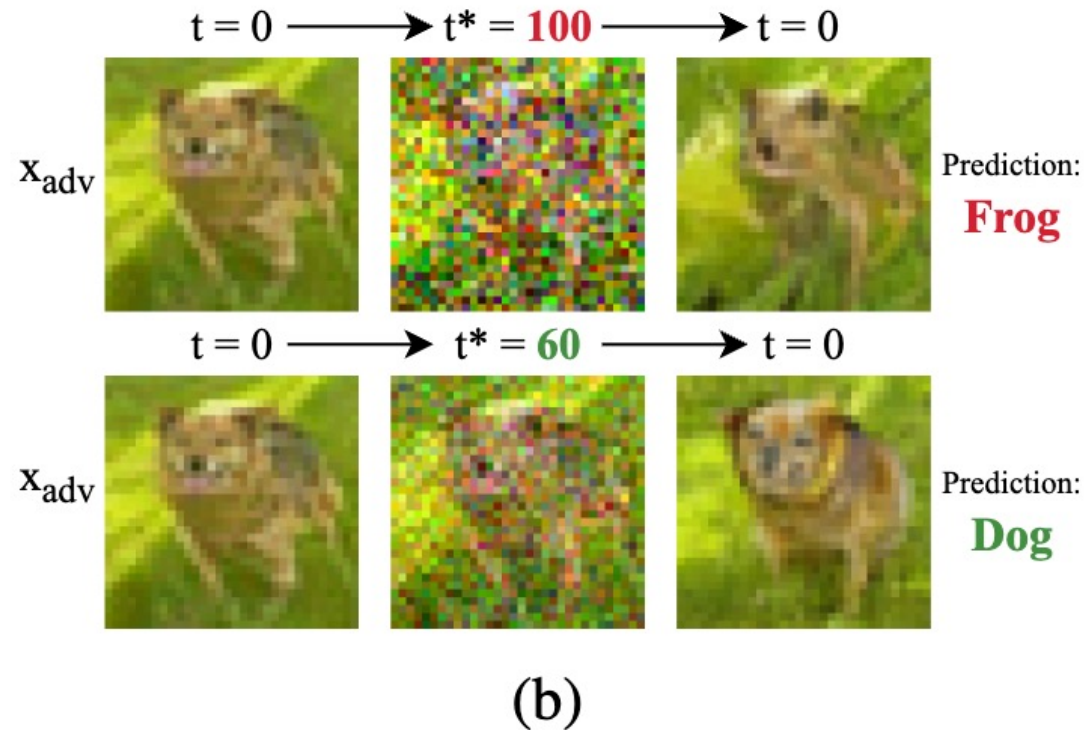
A Key Challenge: The Choice of t

- ❑ If t is too small, then adversarial noise cannot be fully removed.
- ❑ If t is too large, then the purified image may have a different semantic meaning.
- ❑ **Research gap:** current methods empirically select a *fixed* timestep t for all images, which is *counterintuitive*.

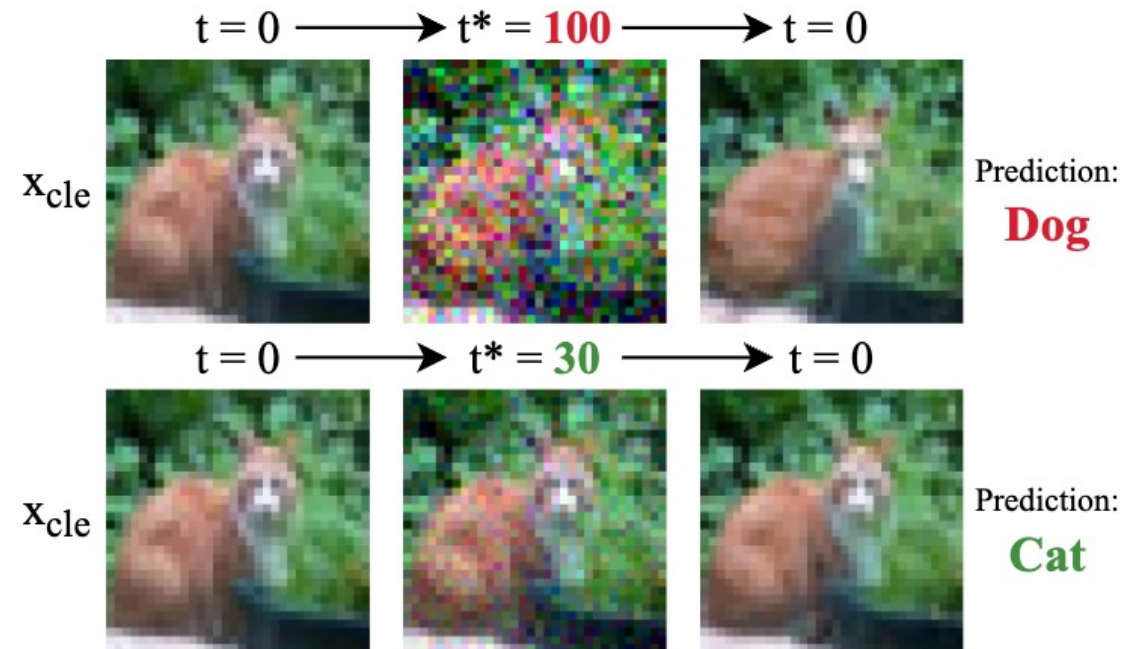


(a)

- ❑ Sample-shared noise level is sometimes **insufficient** to remove adversarial perturbations.



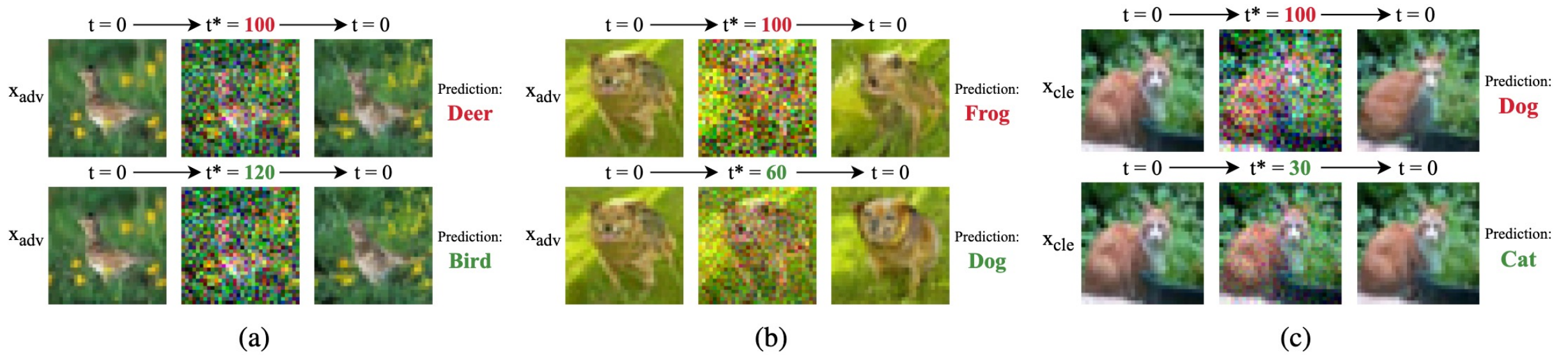
- ❑ Sample-shared noise level is sometimes too **large**, which causes excessive disruption of the sample's semantic information, making it difficult to recover the original semantics.



(c)

- ❑ Sample-shared noise level is often too **large** for clean examples, as they do not need to be purified.

Proof-of-concept Experiment



- ❑ Sample-shared noise level *fail* to address diverse adversarial perturbations.
- ❑ These findings *highlight* the need for sample-specific noise injection levels.

What is the metric?

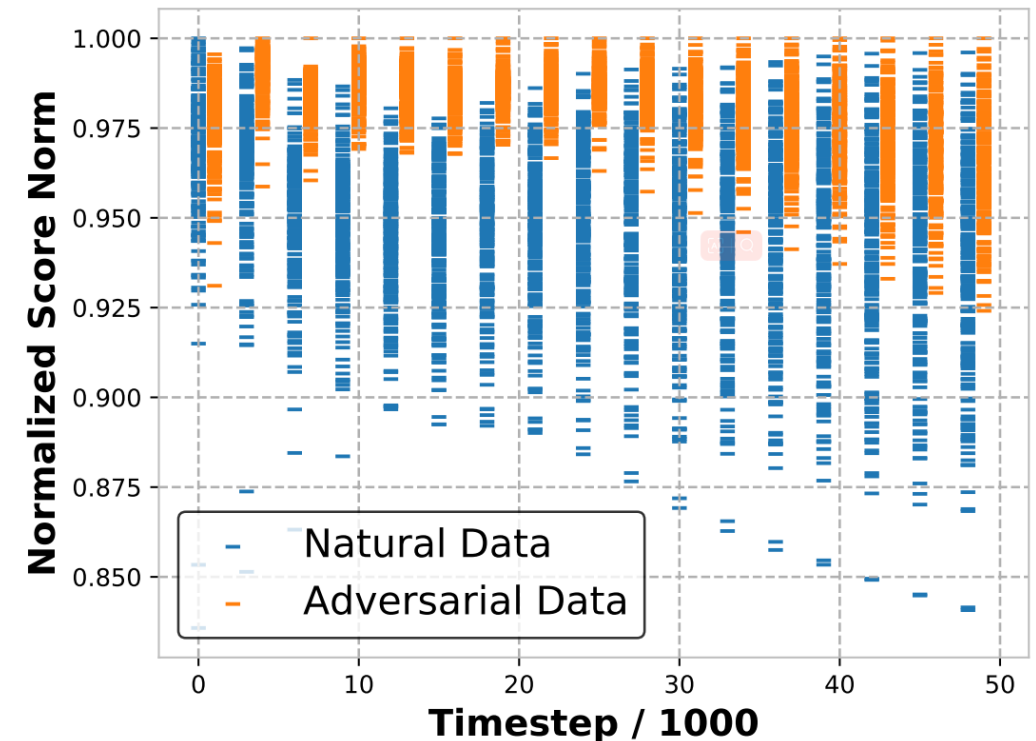
Intuition from score function

Intuition from score function $\nabla_{\mathbf{x}} \log p(\mathbf{x})$

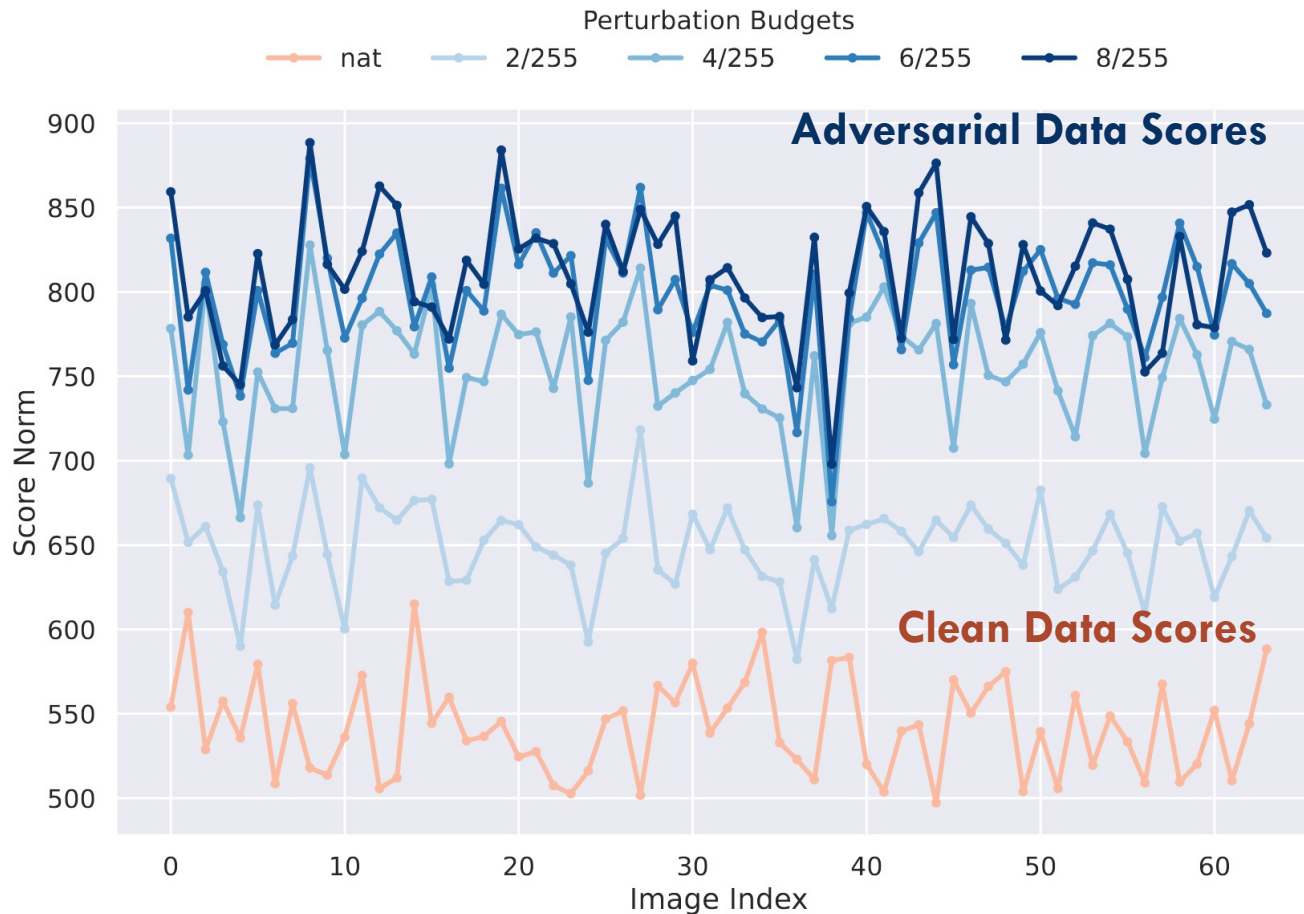
- Score $\nabla_{\mathbf{x}} \log p(\mathbf{x})$ represents the momentum of the sample towards **high density areas** of natural data distribution (Song et al., 2019)



- A **lower score norm** $\|\nabla_{\mathbf{x}} \log p(\mathbf{x})\|$ indicates the sample is **closer** to the high-density areas of natural data distribution

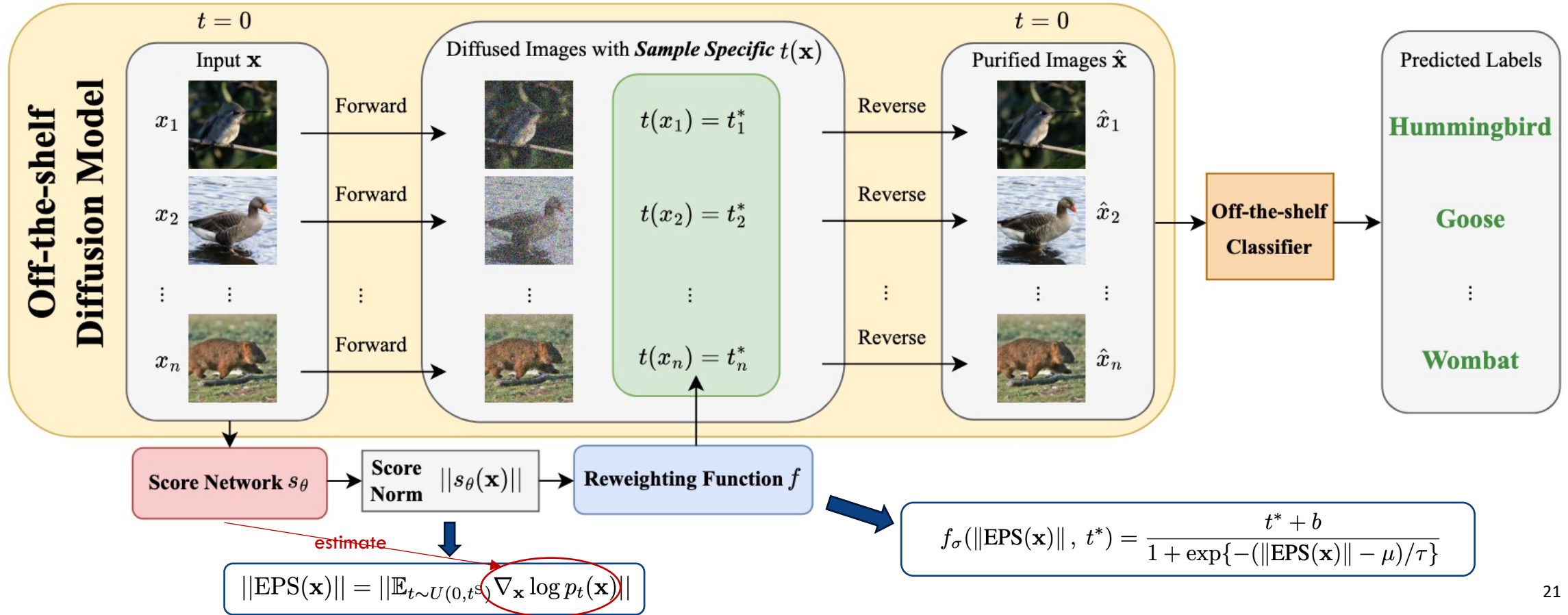


Score norms vs perturbation budgets

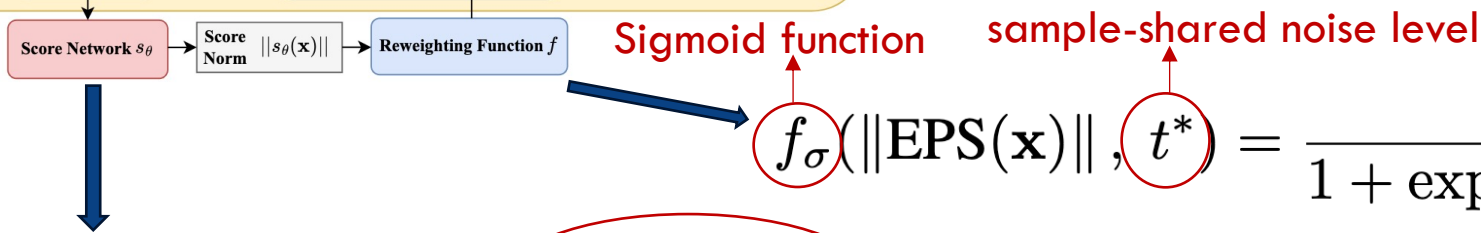
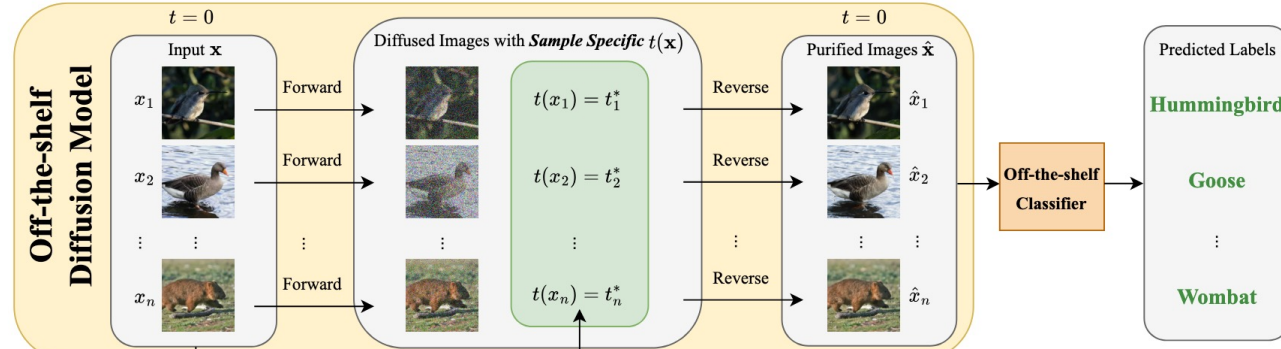


- We further find that score norms *scale directly* with perturbation budgets.
- Score norms can act as *proxies* for estimating the sample-specific noise level.

Sample-specific Score-aware Noise Injection (SSNI)



Sample-specific Score-aware Noise Injection (SSNI)



$$||\text{EPS}(\mathbf{x})|| = ||\mathbb{E}_{t \sim U(0, t^S)} \nabla_{\mathbf{x}} \log p_t(\mathbf{x})||$$

the expectation of the scores of perturbed images across different noise levels $t \sim U(0, t^S)$

$$f_{\sigma}(\|\text{EPS}(\mathbf{x})\|, t^*) = \frac{t^* + b}{1 + \exp\{-(\|\text{EPS}(\mathbf{x})\| - \mu) / \tau\}}$$

bias term
sample-shared noise level
temperature coefficient

mean EPS norm values of clean examples

Main results: CIFAR10

PGD+EOT ℓ_∞ ($\epsilon = 8/255$)			PGD+EOT ℓ_2 ($\epsilon = 0.5$)				
	DBP Method	Standard	Robust		DBP Method	Standard	Robust
WRN-28-10	Nie et al. (2022)	89.71 $\pm$ 0.72	47.98 $\pm$ 0.64	WRN-28-10	Nie et al. (2022)	91.80 $\pm$ 0.84	82.81$\pm$0.97
	+ SSNI-N	93.29$\pm$0.37 (+3.58)	48.63$\pm$0.56 (+0.65)		+ SSNI-N	93.95$\pm$0.70 (+2.15)	82.75 $\pm$ 1.01 (-0.06)
	Wang et al. (2022)	92.45 $\pm$ 0.64	36.72 $\pm$ 1.05		Wang et al. (2022)	92.45 $\pm$ 0.64	82.29 $\pm$ 0.82
	+ SSNI-N	94.08$\pm$0.33 (+1.63)	40.95$\pm$0.65 (+4.23)		+ SSNI-N	94.08$\pm$0.33 (+1.63)	82.49$\pm$0.75 (+0.20)
	Lee & Kim (2023)	90.10 $\pm$ 0.18	56.05 $\pm$ 1.11		Lee & Kim (2023)	90.10 $\pm$ 0.18	83.66 $\pm$ 0.46
	+ SSNI-N	93.55$\pm$0.55 (+2.66)	56.45$\pm$0.28 (+0.40)		+ SSNI-N	93.55$\pm$0.55 (+3.45)	84.05$\pm$0.33 (+0.39)
WRN-70-16	Nie et al. (2022)	90.89 $\pm$ 1.13	52.15 $\pm$ 0.30	WRN-70-16	Nie et al. (2022)	92.90 $\pm$ 0.40	82.94 $\pm$ 1.13
	+ SSNI-N	94.47$\pm$0.51 (+3.58)	52.47$\pm$0.66 (+0.32)		+ SSNI-N	95.12$\pm$0.58 (+2.22)	84.38$\pm$0.58 (+1.44)
	Wang et al. (2022)	93.10 $\pm$ 0.51	43.55 $\pm$ 0.58		Wang et al. (2022)	93.10 $\pm$ 0.51	85.03$\pm$0.49
	+ SSNI-N	95.57$\pm$0.24 (+2.47)	46.03$\pm$1.33 (+2.48)		+ SSNI-N	95.57$\pm$0.24 (+2.47)	84.64 $\pm$ 0.51 (-0.39)
	Lee & Kim (2023)	89.39 $\pm$ 1.12	56.97 $\pm$ 0.33		Lee & Kim (2023)	89.39 $\pm$ 1.12	84.51 $\pm$ 0.37
	+ SSNI-N	93.82$\pm$0.24 (+4.44)	57.03$\pm$0.28 (+0.06)		+ SSNI-N	93.82$\pm$0.24 (+4.43)	84.83$\pm$0.33 (+0.32)

Main results: ImageNet-1K

PGD+EOT ℓ_∞ ($\epsilon = 4/255$)		
DBP Method	Standard	Robust
RN-50	Nie et al. (2022)	68.23 $\pm$ 0.92
	+ SSNI-N	30.34 $\pm$ 0.72
		70.25$\pm$0.56 (+2.02)
		33.66$\pm$1.04 (+3.32)
	Wang et al. (2022)	74.22 $\pm$ 0.12
	+ SSNI-N	0.39 $\pm$ 0.03
		75.07$\pm$0.18 (+0.85)
		5.21$\pm$0.24 (+4.82)
	Lee & Kim (2023)	70.18 $\pm$ 0.60
	+ SSNI-N	42.45 $\pm$ 0.92
		72.69$\pm$0.80 (+2.51)
		43.48$\pm$0.25 (+1.03)

AutoAttack, DiffAttack and Diff-PGD

ℓ_∞ ($\epsilon = 8/255$)					
DBP Method		Standard	AutoAttack	DiffAttack	Diff-PGD
WRN-28-10	Nie et al. (2022)	89.71±0.72	66.73±0.21	47.16±0.48	54.95±0.77
	+ SSNI-N	93.29±0.37 (+3.58)	66.94±0.44 (+0.21)	48.15±0.22 (+0.99)	56.10±0.35 (+1.15)
	Wang et al. (2022)	92.45±0.64	64.48±0.62	54.27±0.72	41.45±0.60
	+ SSNI-N	94.08±0.33 (+1.63)	66.53±0.46 (+2.05)	55.81±0.33 (+1.54)	42.91±0.56 (+1.46)
	Lee & Kim (2023)	90.10±0.18	69.92±0.30	56.04±0.58	59.02±0.28
	+ SSNI-N	93.55±0.55 (+3.45)	72.27±0.19 (+2.35)	56.80±0.41 (+0.76)	61.43±0.58 (+2.41)

Inference Time

DBP Method	Noise Injection Method	Time (s)	DBP Method	Noise Injection Method	Time (s)
Nie et al. (2022)	-	3.934	Nie et al. (2022)	-	8.980
	SSNI-L	4.473		SSNI-L	14.515
	SSNI-N	4.474		SSNI-N	14.437
Wang et al. (2022)	-	5.174	Wang et al. (2022)	-	11.271
	SSNI-L	5.793		SSNI-L	16.657
	SSNI-N	5.829		SSNI-N	16.747
Lee & Kim (2023)	-	14.902	Lee & Kim (2023)	-	35.091
	SSNI-L	15.624		SSNI-L	40.526
	SSNI-N	15.534		SSNI-N	40.633

Limitations of DBP framework & SSNI

- ❑ **Limitation 1:** Having a pre-trained diffusion model is not always feasible, training a diffusion model is resource-consuming.
- ❑ **Limitation 2:** The inference speed of DBP-based methods is slow.
- ❑ **Limitation 3:** SSNI still injects noise to clean samples, which cannot fully preserve the utility (i.e., clean accuracy) of the model.

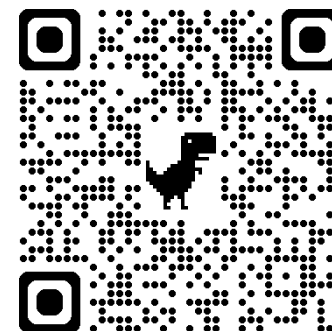
One Stone, Two Birds: Enhancing Adversarial Defense Through the Lens of Distributional Discrepancy

Jiacheng Zhang, Benjamin I. P. Rubinstein, Jingfeng Zhang, Feng Liu*

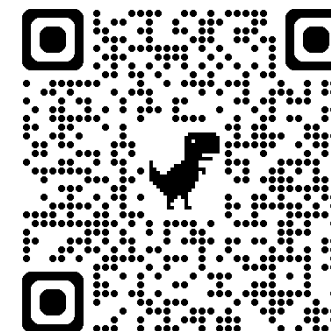
(* Corresponding authors)

In *ICML*, 2025.

Paper



Code



Distributional discrepancy minimization improves robustness

Theorem 1. *For a hypothesis $h \in \mathcal{H}$ and a distribution $\mathcal{D}_A \in \mathbb{D}$:*

$$R(h, f_A, \mathcal{D}_A) \leq R(h, f_C, \mathcal{D}_C) + d_1(\mathcal{D}_C, \mathcal{D}_A).$$

risk on adversarial data **risk on clean data** **distributional discrepancy**

Distributional discrepancy minimization improves robustness

❑ Previous Studies: loose bound due to **an extra constant**

$$R(h, f_{\mathcal{A}}, \mathcal{D}_{\mathcal{A}}) \leq R(h, f_{\mathcal{C}}, \mathcal{D}_{\mathcal{C}}) + d_1(\mathcal{D}_{\mathcal{C}}, \mathcal{D}_{\mathcal{A}}) + \mathbf{C}$$

❑ Ours: **tight bound** without extra constants

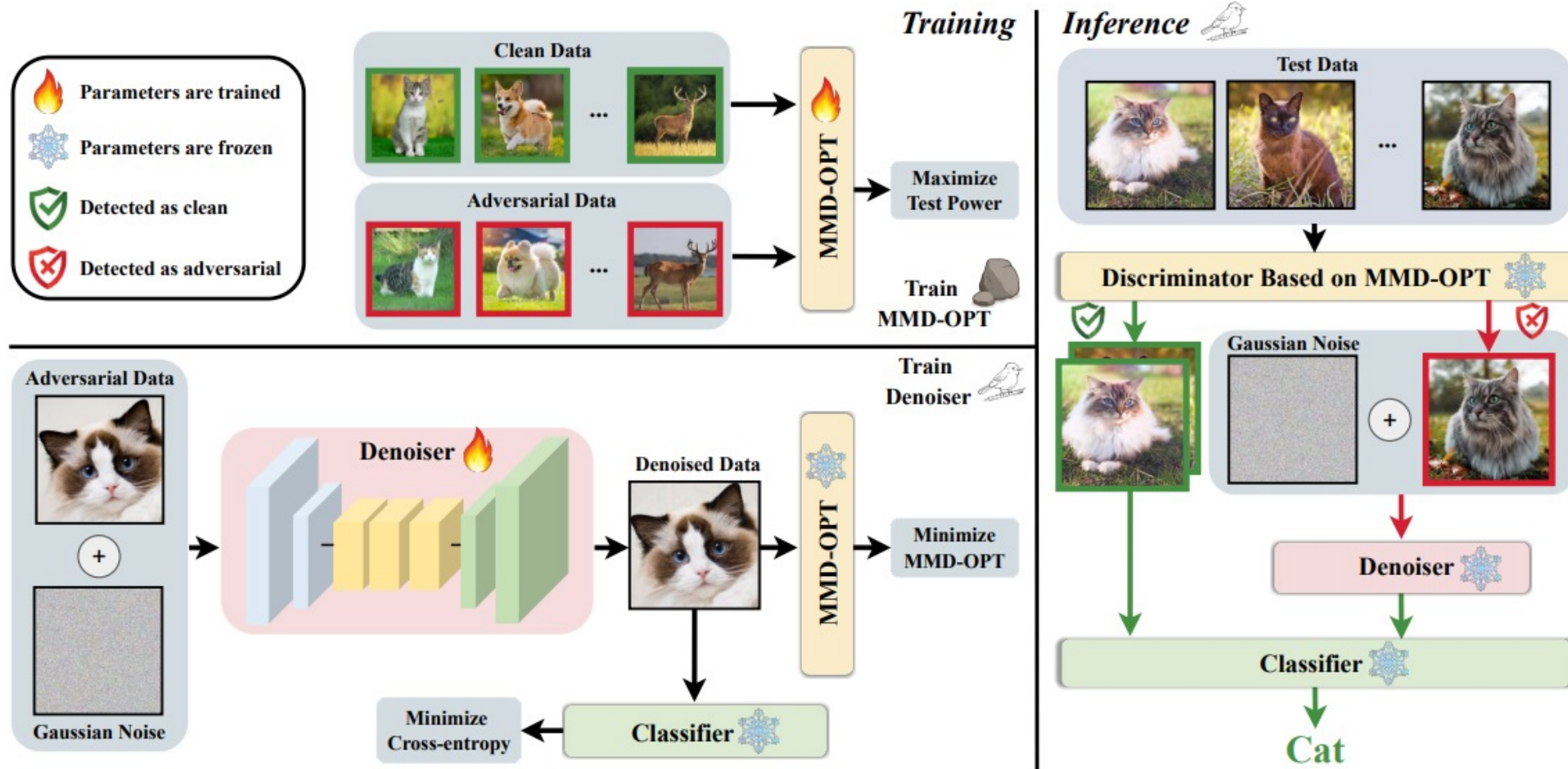
$$R(h, f_{\mathcal{A}}, \mathcal{D}_{\mathcal{A}}) \leq R(h, f_{\mathcal{C}}, \mathcal{D}_{\mathcal{C}}) + d_1(\mathcal{D}_{\mathcal{C}}, \mathcal{D}_{\mathcal{A}})$$

↓
↓
↓

risk on adversarial data
very low if h is a well-trained classifier
distributional discrepancy

≤

Distributional-discrepancy-based Adversarial Defense (DAD)

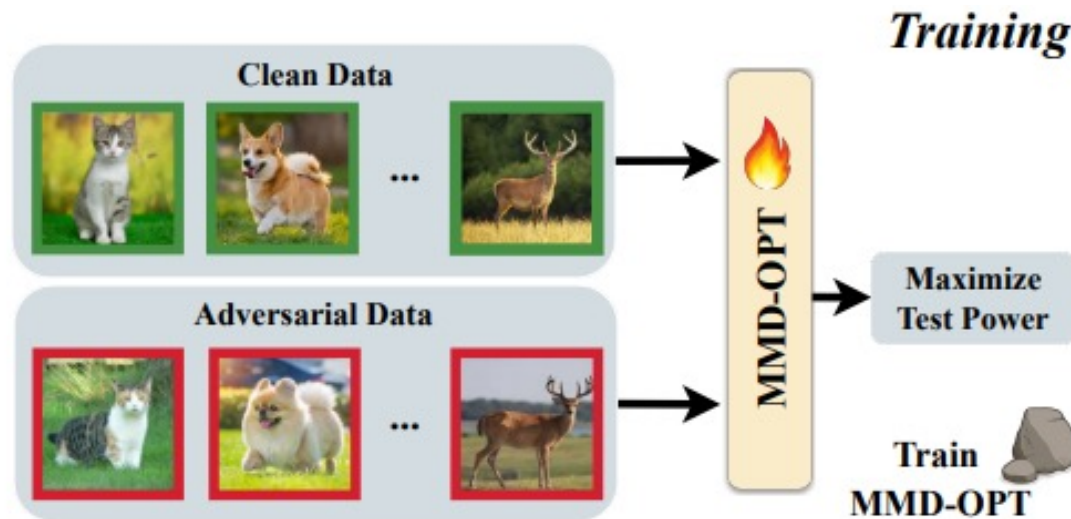


One stone: optimized MMD

$$\text{MMD-OPT}(S'_X, S'_Z) = \widehat{\text{MMD}}^2_u(S'_X, S'_Z; k_\omega^*)$$

MMD values

**0 if same distribution
1 if different**



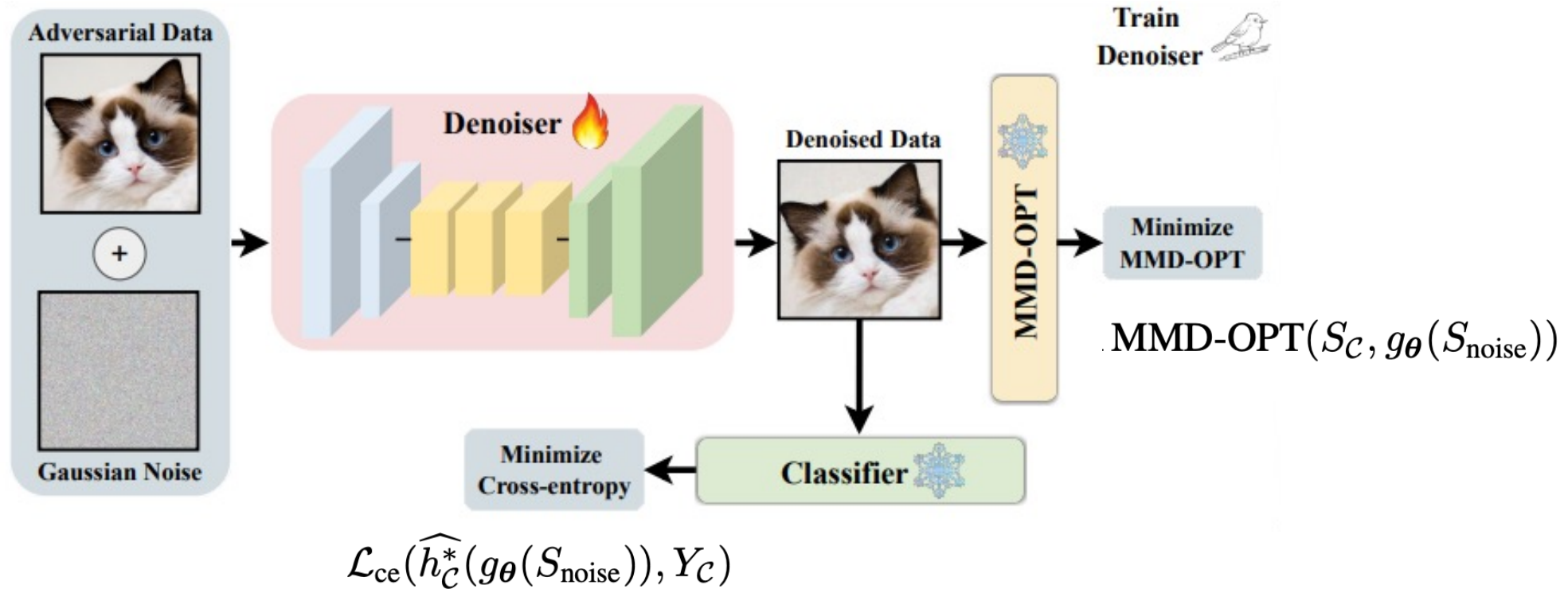
Algorithm 1 Optimizing MMD (Liu et al., 2020).

- 1: **Input:** clean data S_C^{train} , adversarial data S_A^{train} , learning rate η , epoch T ;
- 2: Initialize $\omega \leftarrow \omega_0$; $\lambda \leftarrow 10^{-8}$;
- 3: **for** epoch = 1, ..., T **do**
- 4: $S'_C \leftarrow$ minibatch from S_C^{train} ;
- 5: $S'_A \leftarrow$ minibatch from S_A^{train} ;
- 6: $k_\omega \leftarrow$ kernel function with parameters ω using Eq. (3);
- 7: $M(\omega) \leftarrow \widehat{\text{MMD}}^2_u(S'_C, S'_A; k_\omega)$ using Eq. (2);
- 8: $V_\lambda(\omega) \leftarrow \hat{\sigma}_\lambda(S'_C, S'_A; k_\omega)$ using Eq. (5);
- 9: $\hat{J}_\lambda(\omega) \leftarrow M(\omega) / \sqrt{V_\lambda(\omega)}$ using Eq. (4);
- 10: $\omega \leftarrow \omega + \eta \nabla_{\text{Adam}} \hat{J}_\lambda(\omega)$;
- 11: **end for**
- 12: **Output:** k_ω^*

MMD-OPT serves as:

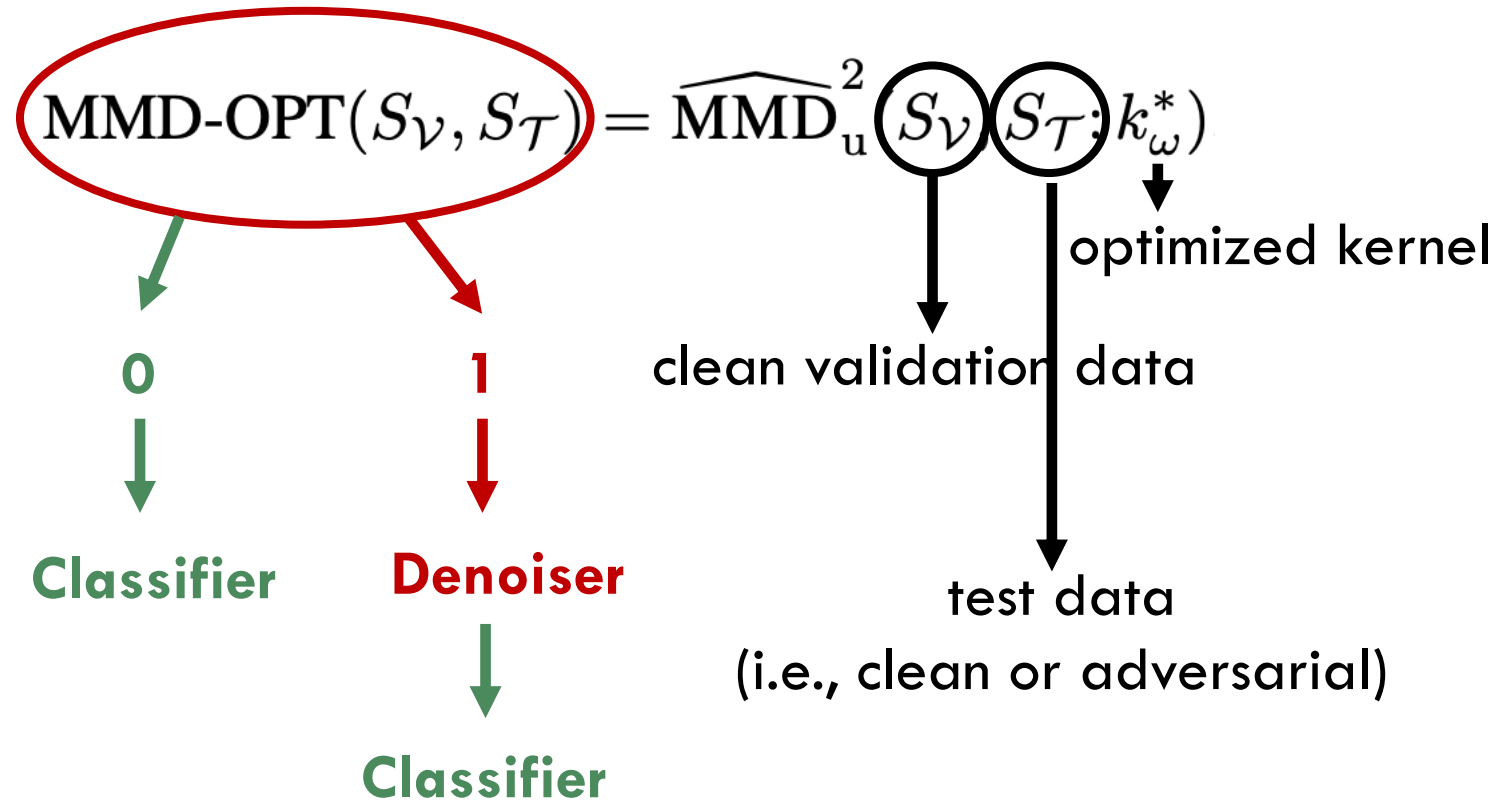
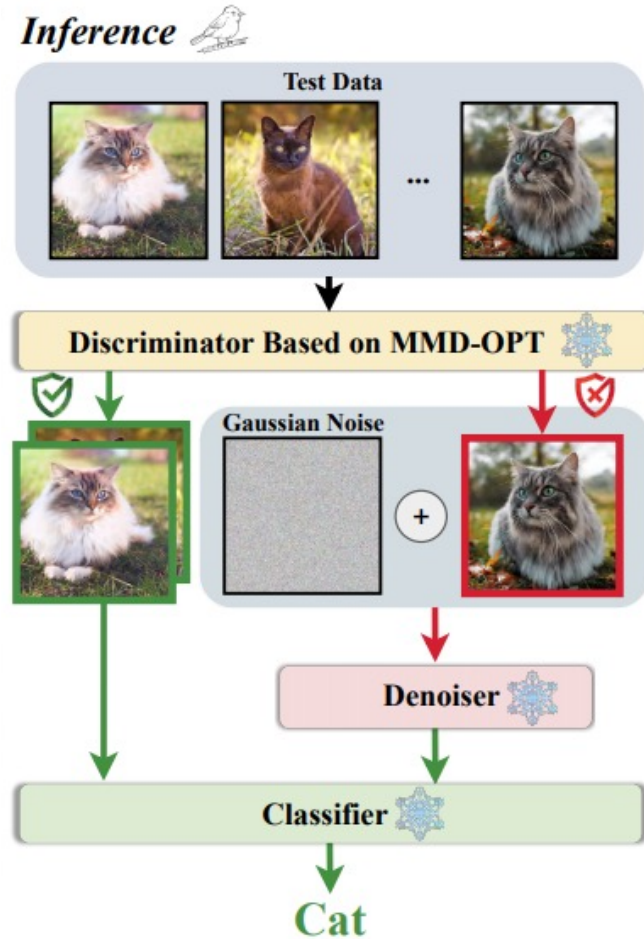
1. **Guiding signal** to train a denoiser.
2. **Discriminator** to differentiate clean data and adversarial data during inference

First bird: MMD-OPT-based denoiser



Objective:
$$g_{\theta^*} = \arg \min_{\theta} \text{MMD-OPT}(S_C, g_\theta(S_{\text{noise}})) + \alpha \cdot \mathcal{L}_{\text{ce}}(\widehat{h}_C^*(g_\theta(S_{\text{noise}})), Y_C)$$

Second bird: MMD-OPT-based discriminator



Adaptive Attack based on PGD+EOT

Algorithm 3 Adaptive white-box PGD+EOT attack for DAD.

```

1: Input: clean data-label pairs  $(S_C, Y_C)$ , optimized characteristic kernel  $k_\omega^*$  by Algorithm 1, pre-trained classifier  $\widehat{h}_C^*$ , denoiser  $g$  with parameters  $\theta$ , maximum allowed perturbation  $\epsilon$ , step size  $\eta$ , PGD iteration  $T$ , EOT iteration  $K$ ;
2: Initialize adversarial data  $S_A \leftarrow S_C$ ;  $\mu \leftarrow 0$ ;  $\sigma \leftarrow 0.25$ ;  $\alpha \leftarrow 10^{-2}$ ;  $t \leftarrow 0.05$ ;
3: for PGD iteration  $1, \dots, T$  do
4:   Initialize gradients over EOT  $\mathcal{G}_{\text{EOT}} \leftarrow \mathbf{0}$ ;
5:   Compute  $\text{MMD-OPT}(S_C, S_A)$  by Eq. (6);
6:   for EOT iteration  $1, \dots, K$  do
7:     if  $\text{MMD-OPT}(S_C, S_A) < t$  then
8:        $\mathcal{G}_{\text{EOT}} \leftarrow \mathcal{G}_{\text{EOT}} + \nabla_{S_A} (\text{MMD-OPT}(S_C, S_A) + \alpha \cdot \mathcal{L}_{\text{ce}}(\widehat{h}_C^*(S_A), Y_C))$ ;
9:     else

```

```

9:     else
10:      Generate Gaussian noise:  $\mathbf{n} \sim \mathcal{N}(\mu, \sigma^2)$ ;
11:       $S_{\text{noise}} \leftarrow S_A + \mathbf{n}$ ;
12:       $\mathcal{G}_{\text{EOT}} \leftarrow \mathcal{G}_{\text{EOT}} + \nabla_{S_A} (\text{MMD-OPT}(S_C, S_A) + \alpha \cdot \mathcal{L}_{\text{ce}}(\widehat{h}_C^*(g_\theta(S_{\text{noise}})), Y_C))$ ;
13:    end if
14:  end for
15:   $\mathcal{G}_{\text{EOT}} \leftarrow \frac{1}{K} \mathcal{G}_{\text{EOT}}$ ;
16:  Update  $S_A \leftarrow \Pi_{\mathcal{B}_\epsilon(S_C)}(S_A + \eta \cdot \text{sign}(\mathcal{G}_{\text{EOT}}))$ ;
17: end for
18: Output:  $S_A$ 

```

Aims to mislead MMD-OPT,
and then, mislead the denoiser and the
classifier correspondingly

Main results: CIFAR-10

ℓ_∞ ($\epsilon = 8/255$)				ℓ_2 ($\epsilon = 0.5$)			
Type	Method	Clean	Robust	Type	Method	Clean	Robust
WRN-28-10				WRN-28-10			
AT	Gowal et al. (2021)	87.51	63.38	AT	Rebuffi et al. (2021)*	91.79	78.80
	Gowal et al. (2020)*	88.54	62.76		Augustin et al. (2020) [†]	93.96	78.79
	Pang et al. (2022a)	88.62	61.04		Schwag et al. (2022) [†]	90.93	77.24
AP	Yoon et al. (2021)	85.66	33.48	AP	Yoon et al. (2021)	85.66	73.32
	Nie et al. (2022)	90.07	46.84		Nie et al. (2022)	91.41	79.45
	Lee & Kim (2023)	90.16	55.82		Lee & Kim (2023)	90.16	83.59
Ours	DAD	94.16 ± 0.08	67.53 ± 1.07	Ours	DAD	94.16 ± 0.08	84.38 ± 0.81
WRN-70-16				WRN-70-16			
AT	Rebuffi et al. (2021)*	92.22	66.56	AT	Rebuffi et al. (2021)*	95.74	82.32
	Gowal et al. (2021)	88.75	66.10		Gowal et al. (2020)*	94.74	80.53
	Gowal et al. (2020)*	91.10	65.87		Rebuffi et al. (2021)	92.41	80.42
AP	Yoon et al. (2021)	86.76	37.11	AP	Yoon et al. (2021)	86.76	75.66
	Nie et al. (2022)	90.43	51.13		Nie et al. (2022)	92.15	82.97
	Lee & Kim (2023)	90.53	56.88		Lee & Kim (2023)	90.53	83.57
Ours	DAD	93.91 ± 0.11	67.68 ± 0.87	Ours	DAD	93.91 ± 0.11	84.03 ± 0.75

Main results: ImageNet-1K

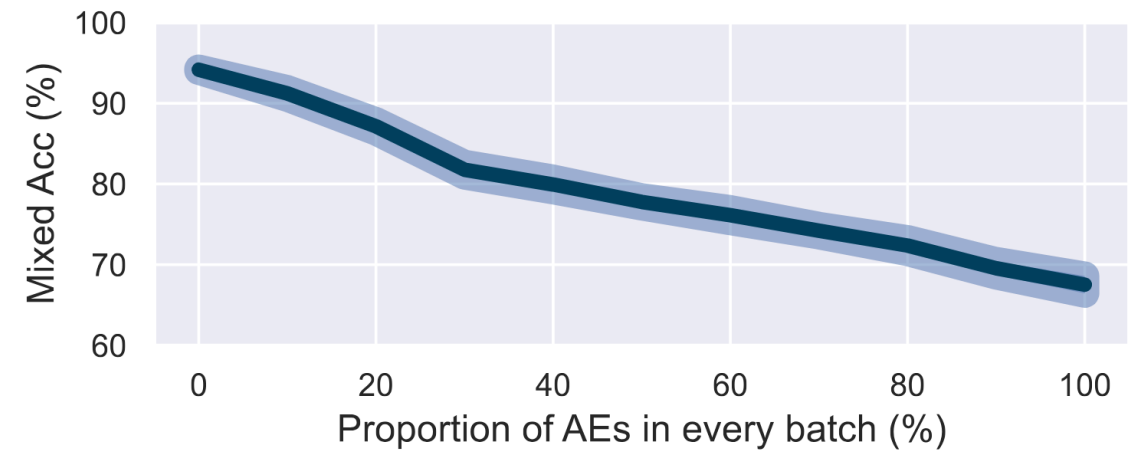
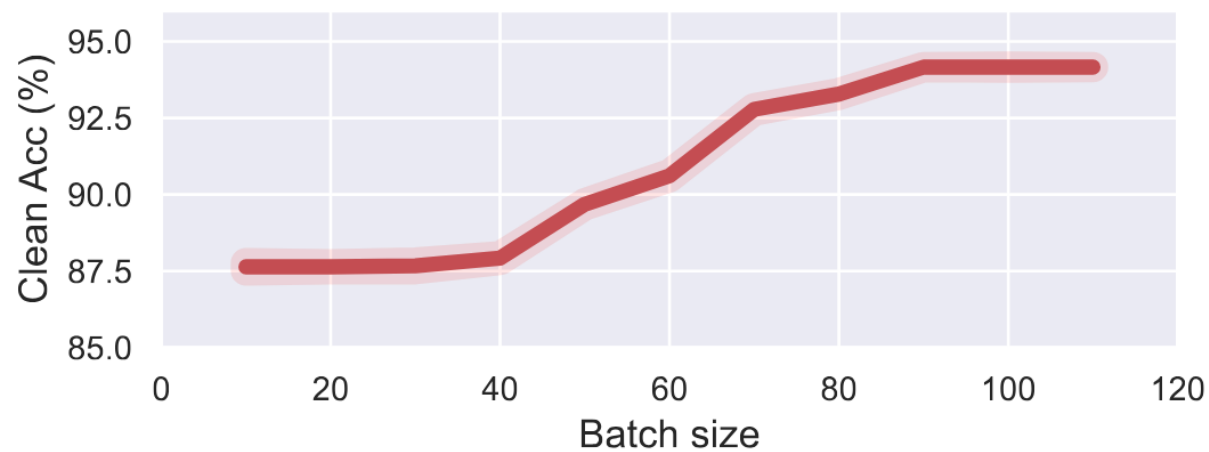
ℓ_∞ ($\epsilon = 4/255$)			
Type	Method	Clean	Robust
RN-50			
AT	Salman et al. (2020a)	64.02	34.96
	Engstrom et al. (2019)	62.56	29.22
	Wong et al. (2020)	55.62	26.24
AP	Nie et al. (2022)	71.48	38.71
	Lee & Kim (2023)	70.74	42.15
Ours	DAD	78.61 $\pm$ 0.04	53.85 $\pm$ 0.23

Trained on WRN-28-10					
Unseen Transfer Attack		WRN-70-16	RN-18	RN-50	Swin-T
PGD+EOT (ℓ_∞)	$\epsilon = 8/255$	80.84 ± 0.46	80.78 ± 0.60	81.47 ± 0.30	81.46 ± 0.29
	$\epsilon = 12/255$	80.26 ± 0.60	80.54 ± 0.45	80.98 ± 0.36	80.40 ± 0.41
C&W (ℓ_2)	$\epsilon = 0.5$	82.45 ± 0.19	91.30 ± 0.20	89.26 ± 0.11	93.45 ± 0.17
	$\epsilon = 1.0$	81.20 ± 0.39	90.37 ± 0.17	88.65 ± 0.22	93.41 ± 0.18

Strength of DAD

- ❑ **Strength 1:** DAD can largely preserve the original utility (i.e., clean accuracy of the classifier).
- ❑ **Strength 2:** Compared to DBP methods that rely on density estimation, learning distributional discrepancies is a simpler and more feasible task.
- ❑ **Strength 3:** DAD is efficient in both training and inferencing.

Limitations of DAD



Thank You!